



# **Informative Data and Uncertainty in Stock Assessment**

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Ph.D. defense**

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# Outline

## Introduction

Uncertainty in stock assessment, research questions

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## Papers 1 & 2 (simulation studies)

Informative data, stock status, key parameters

Delta method, bootstrap, MCMC

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## **Paper 3 (synthesis and case study)**

Broader overview, application of methods to Icelandic saithe

Profile likelihood, retro, bivariate confidence region, HCR

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Broader overview, application of methods to Icelandic saithe

Profile likelihood, retro, bivariate confidence region, HCR

## **Conclusions**

Summary of findings, general recommendations

## Uncertainty in stock assessment

Fisheries management relies on stock assessment

Stock status, harvest rate, reference points, key parameters

Not just the most likely value, but a range of plausible values

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Fisheries management relies on stock assessment

Stock status, harvest rate, reference points, key parameters

Not just the most likely value, but a range of plausible values

Give advice that is robust to violated assumptions

Failure to incorporate uncertainty into the management advice  
→ suboptimal yields, fishery collapse

## Research questions

What makes some datasets more **informative** than others?



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How reliable are **statistical methods** to measure uncertainty?

What are **good practices** for confronting uncertainty?

# Study design

## Simulation studies 1-2

Generate random datasets where the true values are known

Evaluate the performance of statistical methods

Typical groundfish data and age-structured model

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## Simulation studies 1-2

- Generate random datasets where the true values are known
- Evaluate the performance of statistical methods
- Typical groundfish data and age-structured model

## Review & case study 3

- Review findings from simulation studies
- Apply same methods to Icelandic saithe, interpret results
- Demonstrate additional methods to confront uncertainty

## Paper 1

FISH and FISHERIES, 2007, 8, 337–358

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### **What makes fisheries data informative?**

*Arni Magnusson<sup>1,2</sup> & Ray Hilborn<sup>1</sup>*

## Paper 1

FISH and FISHERIES, 2007, 8, 337–358

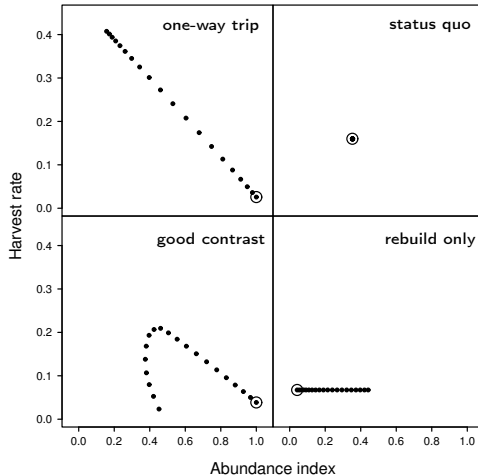
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### What makes fisheries data informative?

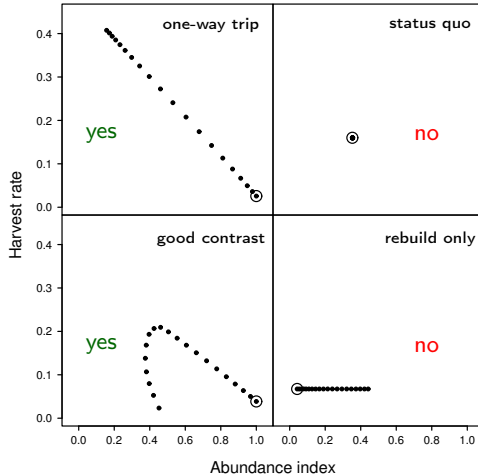
*Arni Magnusson<sup>1,2</sup> & Ray Hilborn<sup>1</sup>*



# Informative fishing history?

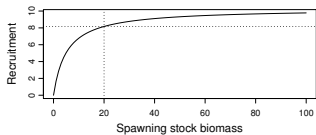


# Informative fishing history?



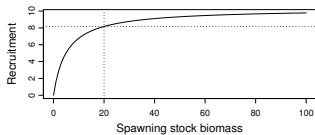


# Key parameters: $h$ , $M$ , $r$



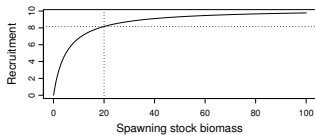
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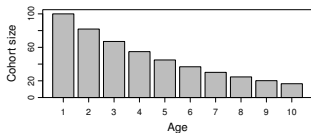


$h$  : stock-recruitment steepness  
only if data include very low *SSB*

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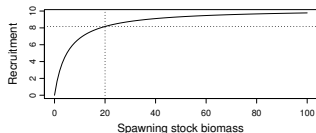


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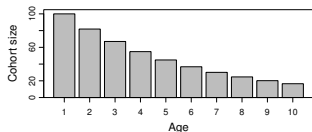


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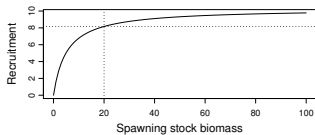


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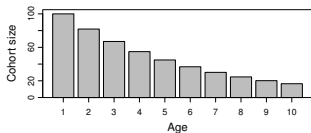


$M$  : natural mortality rate  
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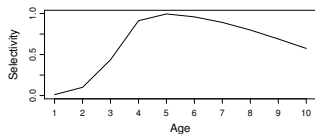
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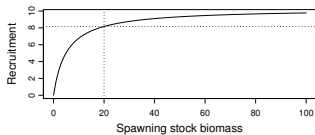


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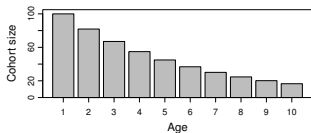


$r$  : right-hand selectivity

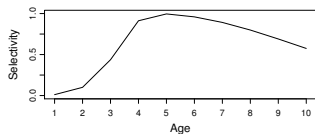
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$h$  : stock-recruitment steepness  
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$r$  : right-hand selectivity  
confounded with  $M$

## Paper 2

FISH and FISHERIES, 2013, **14**, 325–342

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### **Measuring uncertainty in fisheries stock assessment: the delta method, bootstrap, and MCMC**

*Arni Magnusson<sup>1,2</sup>, André E Punt<sup>1</sup> & Ray Hilborn<sup>1</sup>*

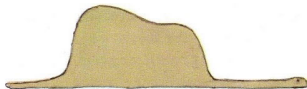
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# Uncertainty methods: delta, boot, mcmc

## Procedure

## Interval

Delta  
method

$$\widehat{\text{SE}}_{\hat{g}} = \sqrt{\sum_i \sum_j \widehat{\text{Cov}}(\hat{\theta}_i, \hat{\theta}_j) \left(\frac{\partial g}{\partial \theta_i}\right) \left(\frac{\partial g}{\partial \theta_j}\right)}$$

$$\left[ \hat{g} - z_{1-\alpha/2} \widehat{\text{SE}}_{\hat{g}}, \hat{g} + z_{1-\alpha/2} \widehat{\text{SE}}_{\hat{g}} \right]$$

Bootstrap

simulate datasets  $\mathbf{y}^*$

$$\left[ \frac{\alpha}{2} \text{ quantile from } {}_{\text{BC}}\vec{\theta}^*, \left(1 - \frac{\alpha}{2}\right) \text{ quantile from } {}_{\text{BC}}\vec{\theta}^* \right]$$

MCMC

simulate parameter values

$$\left[ \frac{\alpha}{2} \text{ quantile from } \vec{\theta}, \left(1 - \frac{\alpha}{2}\right) \text{ quantile from } \vec{\theta} \right]$$

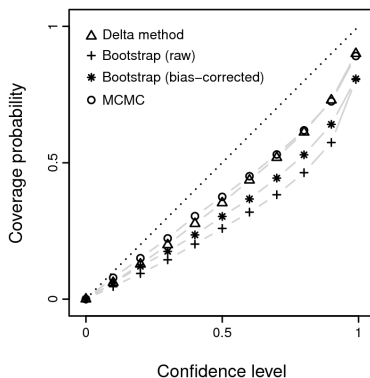
# Uncertainty methods: delta, boot, mcmc

## Performance

Delta  
method

Bootstrap

MCMC



# Uncertainty methods: delta, boot, mcmc

## Performance

Delta  
method

Bootstrap

MCMC

All methods  
produce  
too narrow  
intervals

Better than  
bootstrap

Better than  
bootstrap

Best in terms of  
worst-case  
performance

## Paper 3

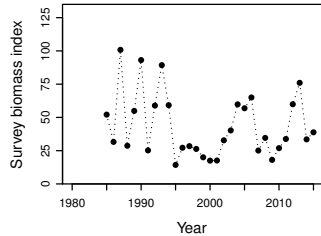
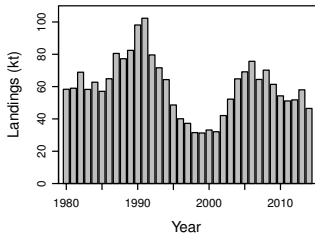
# Confronting Uncertainty in Stock Assessment

## Paper 3

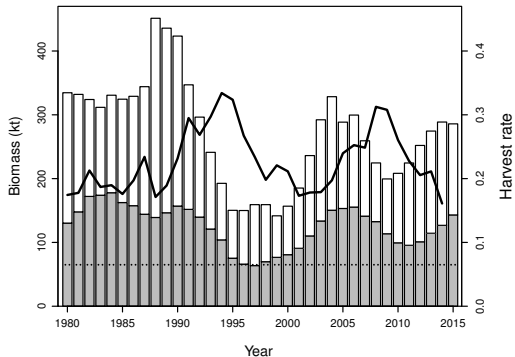
# Confronting Uncertainty in Stock Assessment



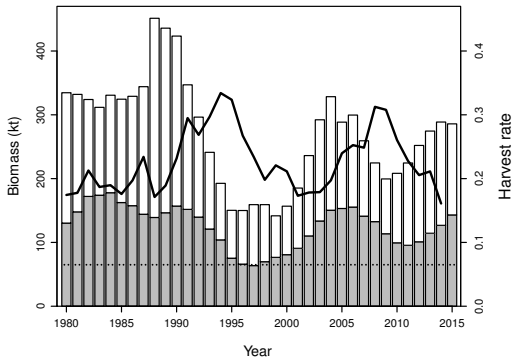
# Icelandic saithe



# Biomass and harvest rate



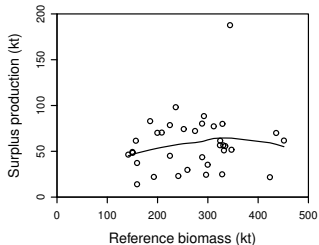
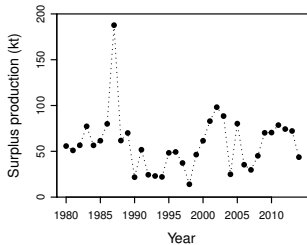
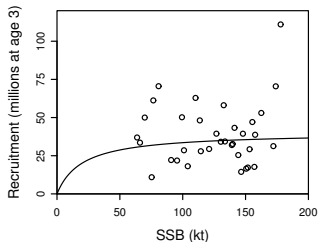
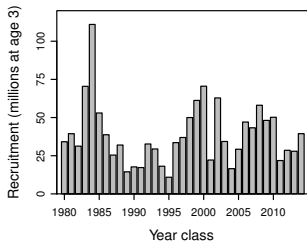
## Biomass and harvest rate



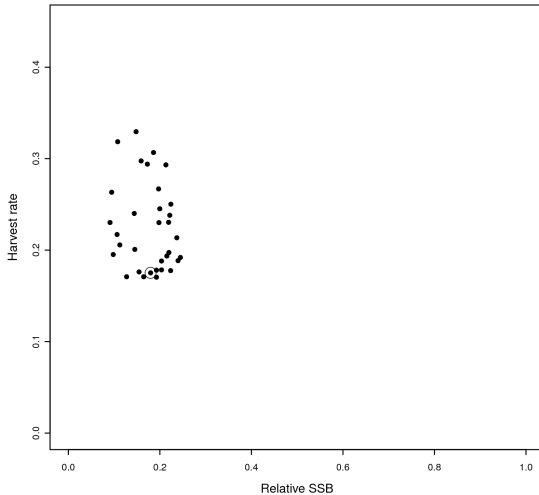
$$20\% \text{ HCR: } TAC_t = \frac{0.20B_{t,4+} + TAC_{t-1}}{2}$$



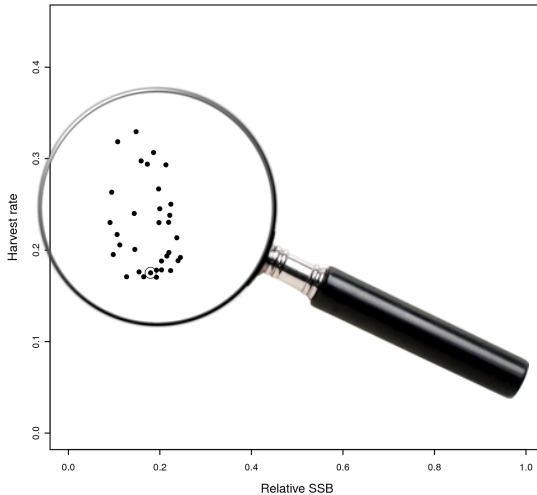
# Recruitment and surplus production



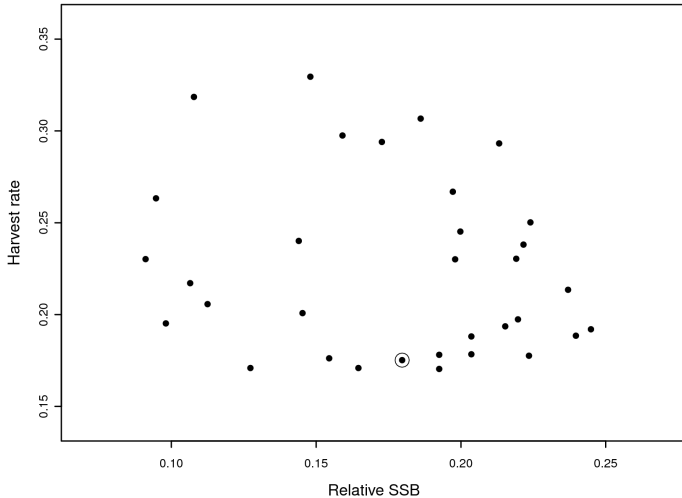
# Fishing history



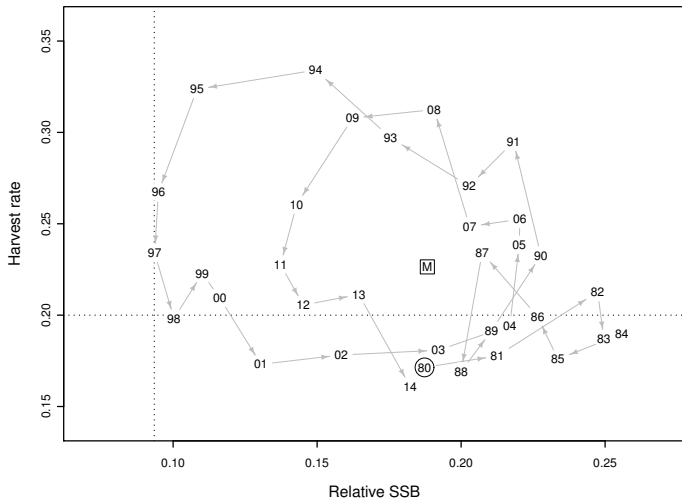
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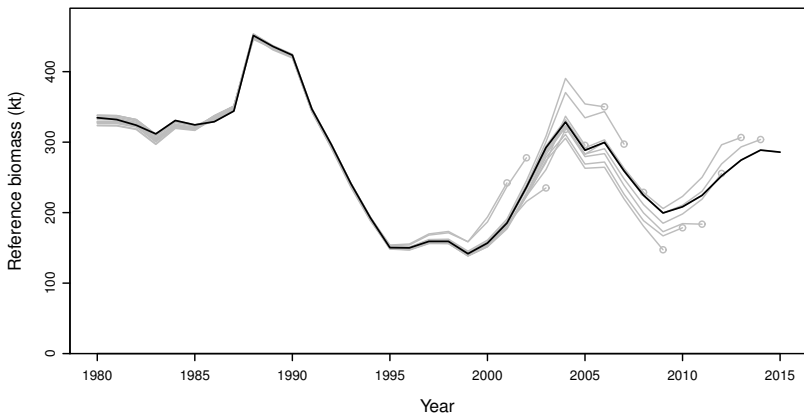
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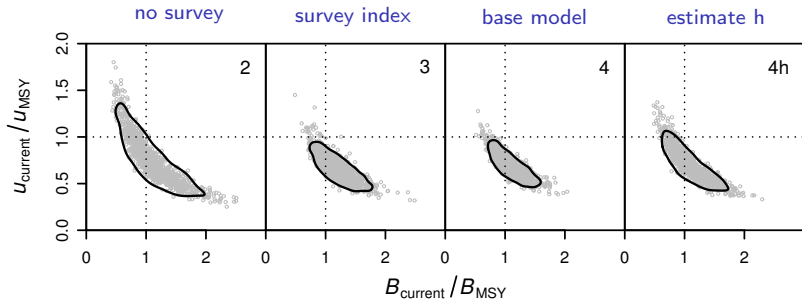
# Fishing history



## Retrospective analysis

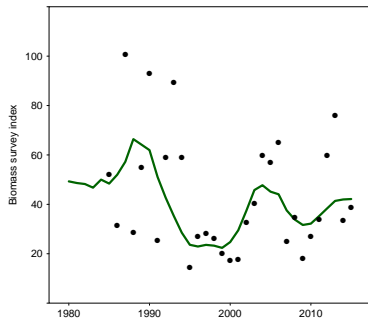


# Bivariate confidence region

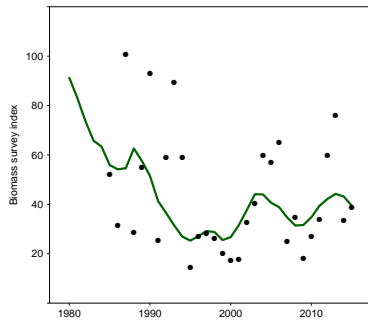


# Estimating $M$

Base model  $M = 0.2$



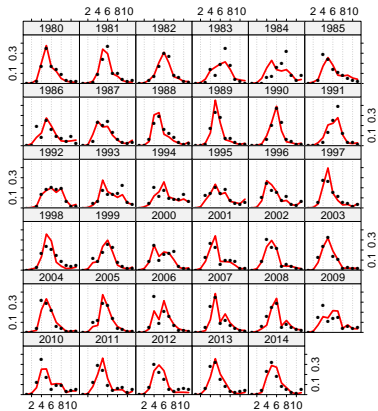
Estimated  $M = 0.57$



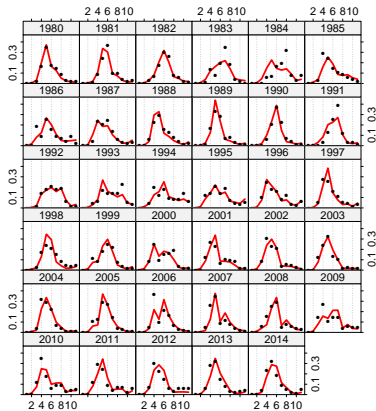


# Estimating $M$

Base model  $M = 0.2$



Estimated  $M = 0.57$



## Estimating $h$ and $M$

### Stock-recruitment steepness

$h = 0.90$  in base model

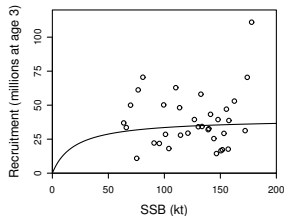
Point estimate is 0.99

## Estimating $h$ and $M$

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### Stock-recruitment steepness

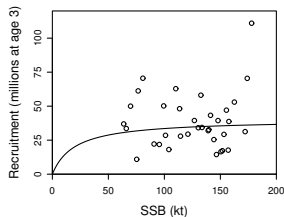
$h = 0.90$  in base model

Point estimate is 0.99

### Natural mortality rate

$M = 0.20$  in base model

Point estimate is 0.57

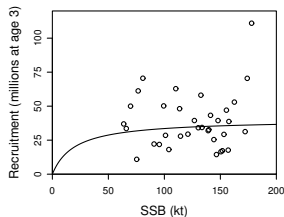


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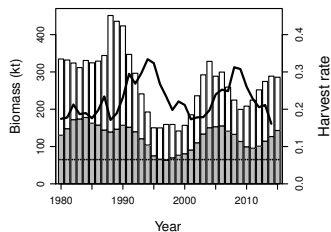
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# Summary of findings

## Fishing history

One-way-trip proved no less informative than good contrast

'the more fish you catch, the better you know how many there were'

## Key parameters

$h$  : data must include years with very low  $SSB$

$M$  : data must include high and low  $F$

$r$  : confounded with  $M$

## Uncertainty methods

MCMC, delta method, profile likelihood more reliable than bootstrap

## General recommendations

- 1 Use more than one method to evaluate uncertainty.
- 2 Keep in mind that the real uncertainty is greater than the analytical confidence intervals indicate.
- 3 Use more than one model and variations of models to evaluate how sensitive the main conclusions are to alternative assumptions.
- 4 Use retrospective analysis to evaluate uncertainty from an empirical viewpoint.

## General recommendations

- 5 Use simulation analysis to evaluate the performance of the estimation model, which parameters can be estimated reliably, and which uncertainty methods work best.
- 6 Examine the fishing history to evaluate whether the data are likely to be informative about the stock status and key parameters like  $h$  and  $M$ .
- 7 Consider ways to reduce uncertainty by generating informative data via management (e.g., applying different fishing mortalities between years) and research (e.g., design a dedicated survey for a given stock, sample age data).
- 8 Harvest control rules can be a practical way to incorporate uncertainty into management advice.



# Value

Comprehensive **overview** and **evaluation**  
of methods to analyze uncertainty

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Comprehensive **overview** and **evaluation**  
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Checklist of **recommendations**  
for stock assessment practitioners

# Acknowledgements

**Committee:** Ray, André, Jim, John, Christine

**Staff:** Amy, Mabelle

**ADMB friends:** Dave, Hans, Johnnoel, Jim, Mark, Anders, John

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Thank you!

